

A Year 9 course based on the New Zealand Mathematics and Statistics Curriculum

# Fast Track 1

## Mathematics Workbook

W. Geldof

Written for able Year 9 students  
aiming to achieve high standards in mathematics

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Second Edition



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## INTRODUCTION

### Information for Teachers and Parents

Fast Track maths workbooks are written for able students, providing them with new mathematical ideas and challenging questions.

The Fast Track 1 workbook revises level 4 and starts level 5 of the New Zealand Mathematics and Statistics Curriculum. Full details of curriculum/chapter links can be found on page A14 at the back of this book.

Students will work at the Advanced Multiplicative and Proportional Stages of the Secondary Numeracy Project (stages 7, 8).

### Tips for Students

- ◆ Never accept the answer on your calculator at face value, check it. Often your answer will need a unit e.g. \$, km, min.
- ◆ Work out difficult questions on scrap paper first and use brief sentences to write any explanations.

Wiesje Geldof