

A Year 10 course based on the New Zealand Mathematics and Statistics Curriculum

# Fast Track 2

## Mathematics Workbook

W. Geldof

Written for able Year 10 students  
aiming to achieve high standards in mathematics

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Second Edition



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**INTRODUCTION**

**Information for Teachers and Parents**

The **Fast Track** maths workbooks are written for **more able** students, providing them with new mathematical ideas and asking challenging questions.

The **Fast Track 2** workbook covers work in **Level 5** of the New Zealand Mathematics and Statistics Curriculum. Full details of curriculum/chapter links can be found on page A14 at the back of this book. Students will be working at the **Proportional Stage** of the Secondary Numeracy Project (stage 8).

**Tips for Students**

- ◆ Never accept the answer on your calculator at face value, check it. Often your answer will need a unit e.g. \$, km, min.
- ◆ Work out difficult questions on scrap paper first and use brief sentences to write any explanations.
- ◆ Save the 'end-of-chapter' test until you are ready to do it without help. The result will indicate any weak areas which need further revision.

*Wiesje Geldof*